Abstract of paper [1].

We prove that if λ_1 , λ_2 , λ_3 and λ_4 are non-zero real numbers, not all of the same sign, λ_1/λ_2 is irrational, and α is any real number then, for any $\varepsilon > 0$ the inequality $|\lambda_1 p_1 + \lambda_2 p_2^2 + \lambda_3 p_3^2 + \lambda_4 p_4^2 - \alpha| \le (\max_j p_j)^{-1/18+\varepsilon}$ has infinitely many solutions in prime variables p_1, \ldots, p_4 .

References

[1] A. Languasco and A. Zaccagnini. A Diophantine problem with a prime and three squares of primes. *J. Number Theory*, 132:3016–3028, 2012.